

Sloppy monomials

(Sethna,)

© 2024, James P. Sethna, all rights reserved.

```
f[x_] := Sin[π (2 x)]
M := 5
fTaylor[x_] = Series[...] // Normal // N // Chop
fChebyshev[x_] = 0.0066 + 5.652 x + 9.701 x2 - 95.455 x3 + 133.48 x4 - 53.39 x5
fLegendre[x_] = 0.016 + 5.410 x + 11.304 x2 - 99.637 x3 + 138.15 x4 - 55.26 x5

Plot[{f[x], fChebyshev[x], ...}, {x, 0, 1}]
Plot[{...}, {x, 0, 1}]
Plot[{...}, ...]

H[n_, m_] := ...
Ham[M_] = Table[H[n, m] // N, ...];
{vals5, vecs5} = Eigensystem[Ham[M]];
conditionNumber = ...
ratios = ...

sloppiest = ...; (* Is it the first row or the first column? *)
sloppyPolynomial[x_] := Sum[... x^n, {n, 0, M}]
sloppyPolynomial[x]
Plot[...]
```