

### Material for Week 3

Physics 4488/6562: Statistical Mechanics

<https://sethna.lassp.cornell.edu/Teaching/562/>

Exercises due Mon. Feb 14

Last correction at January 11, 2022, 9:02 pm

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All exercises are from the second edition of the text: <https://sethna.lassp.cornell.edu/StatMech/EntropyOrderParametersComplexity20.pdf>

#### Monday

In-class question: [3.16](#) *Taste, smell, and  $\mu$*

#### Wednesday

Read: Chapter 4, Sec. 4.1 (Liouville's theorem), Sec. 4.2 (Ergodicity)

Pre-class question: [4.6](#) *Perverse initial conditions*

In-class question: [4.2](#) *Liouville vs. the damped pendulum*

In-class question: [3.11](#) *Maxwell relations*

#### Friday

Read: Chapter 5, Sec. 5.1 (Engines & Heat Death)

Pre-class question: [4.5](#) *No Hamiltonian attractors*

In-class question: [5.1](#) *Life and the heat death of the Universe*

#### Monday

Read: Chapter 5, Sec. 5.2.1 (Entropy of mixing)

Pre-class question: [3.18](#) *Ideal gas glass*

#### Exercises for everyone (4488 and 6562)

[5.8](#) *The Arnol'd cat map.*

[4.8](#) *Jarzynski.* Liouville's theorem applies also to time-dependent Hamiltonians. Jarzynski, and later Crooks, used this to calculate the exact entropy change for a non-equilibrium process. Here we use an ideal gas, compressed non-adiabatically, to illustrate how this exact result is used in practice.

#### Exercises for Graduate Course (6562 only)

[3.14](#) *Pendulum energy shell.*

[4.7](#) *Crooks.* Here we derive the remarkable Crooks relation using Liouville's theorem